

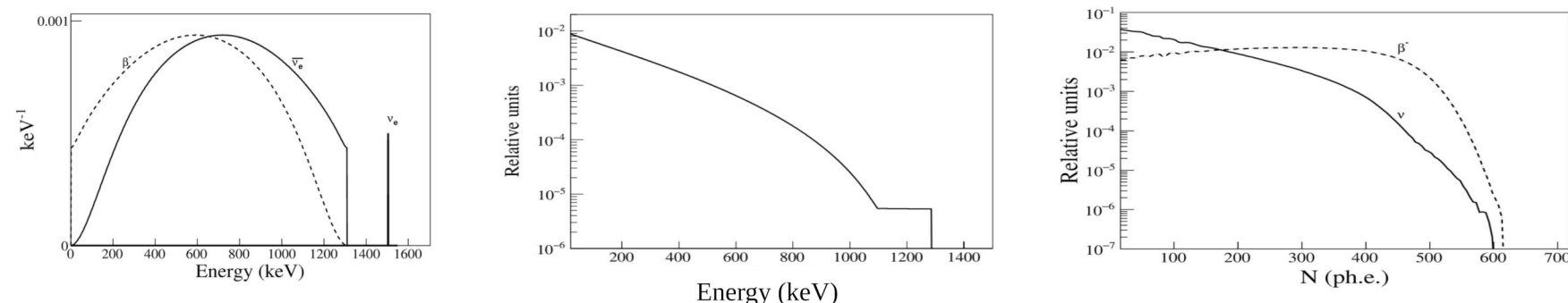
# Potassium influence on Earth's mantle convection and Borexino data.

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### Motivation

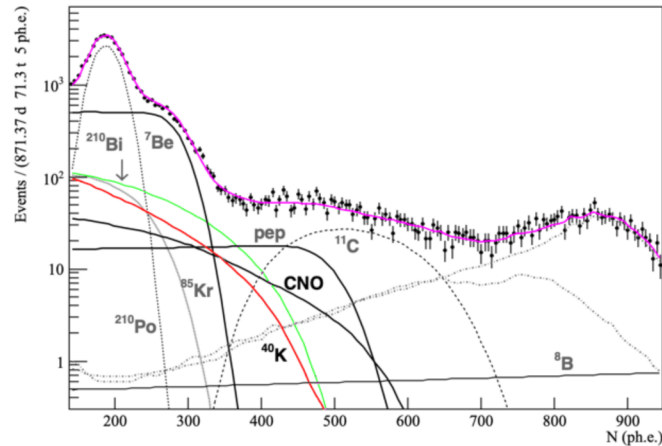
What proportion of potassium in the Earth does Borexino allow?



Antineutrino, beta and neutrino <sup>40</sup>K spectra.

Recoil electron spectrum produced by antineutrinos and neutrinos from <sup>40</sup>K.

PDF for beta and neutrino <sup>40</sup>K.



INR analysis with <sup>40</sup>K account.  
Red line – <sup>40</sup>K spectrum.

$R(\text{CNO}) = 3.9 \pm 1.6$  cpd/100t (low metal model)  
 $R(^{40}\text{K}) = 11 \pm 2$  cpd/100t

$\chi^2 = 175$

### Boussinesq approximation

Thermal convection nondimensionalized equations

We solved the following nondimensionalized equations of mass, momentum, energy, and conservation in 2-D spherical annulus geometry for incompressible mantle flow

$$-\nabla P + \nabla \cdot [\eta(\nabla \mathbf{V} + (\nabla \mathbf{V})^T)] = Ra T \mathbf{e}_r,$$

$$\nabla \cdot \mathbf{V} = 0$$

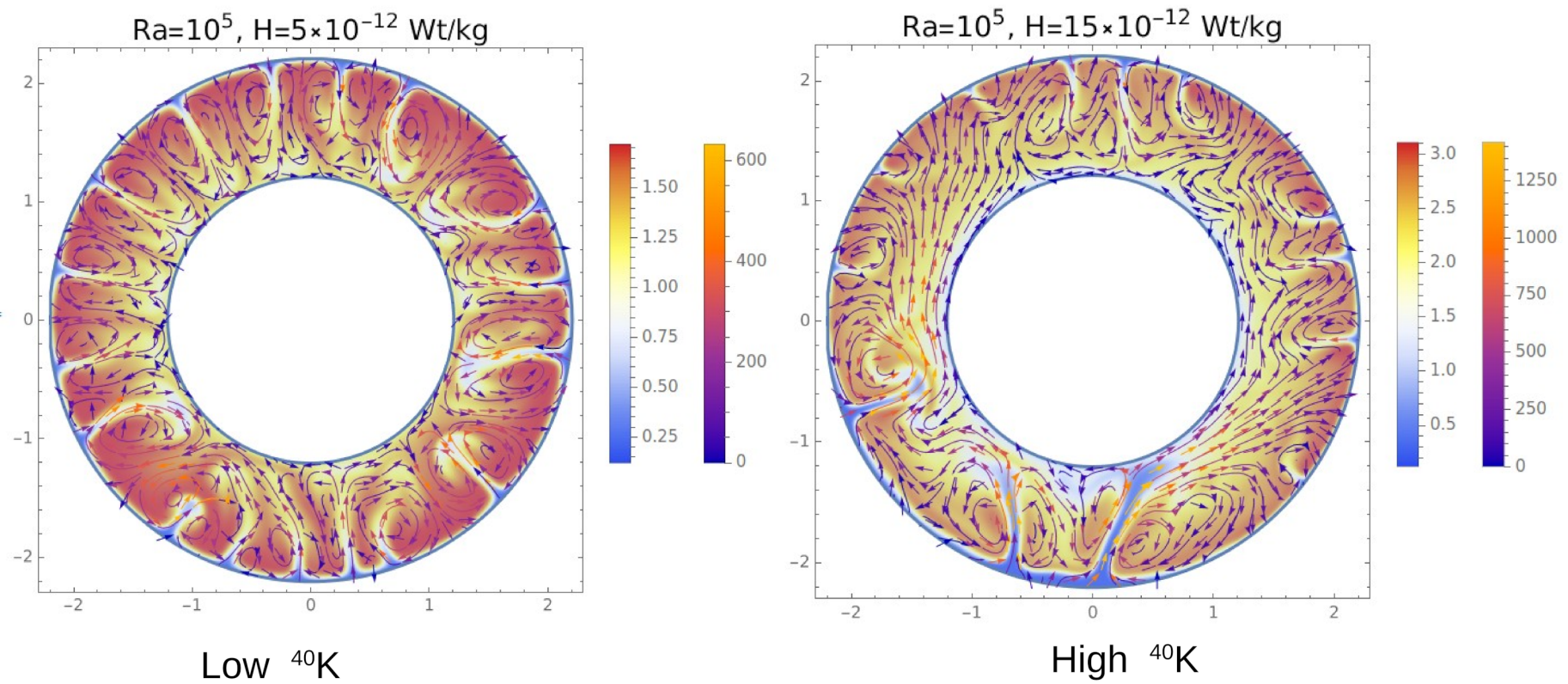
$$\frac{\partial T}{\partial t} + (\mathbf{V} \cdot \nabla) T = \nabla \cdot (\kappa \nabla T) + H(t)$$

Here  $\mathbf{V}$  is the velocity vector,  $P$  is the pressure,  $T$  is the temperature,  $t$  is the time,  $\eta$  is the coefficient of dynamic viscosity,  $\kappa$  is the coefficient of thermal diffusivity,  $H(t)$  is the heat source.  $Ra$  is the Rayleigh number, defined as

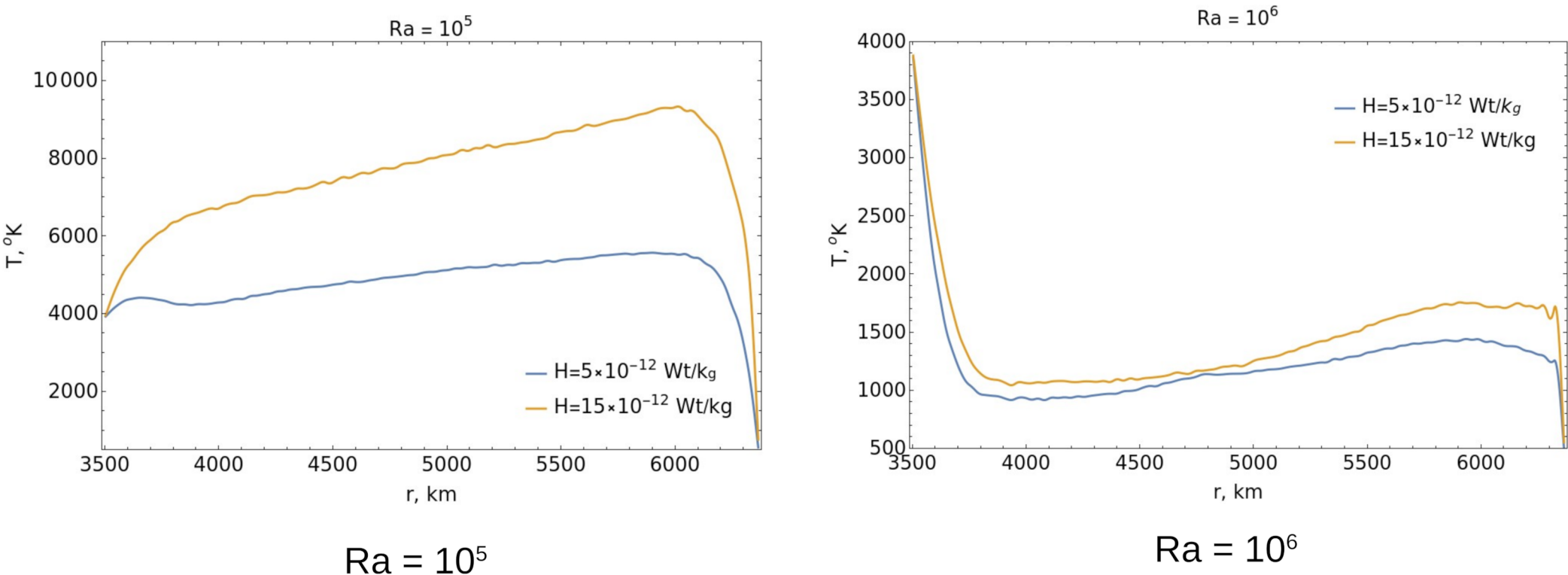
$$Ra = \frac{\alpha \cdot \rho_0 \cdot g \cdot \delta T \cdot D^3}{\eta_0 \cdot \kappa_0}$$

with  $\alpha$  the surface thermal expansivity;  $g$  the gravitational acceleration;  $\Delta T$  the temperature drop across the mantle;  $\rho$  the reference density;  $\eta_0$  the reference viscosity;  $D$  the thickness of the mantle

### Results of mantle convection modeling for $Ra = 10^5$



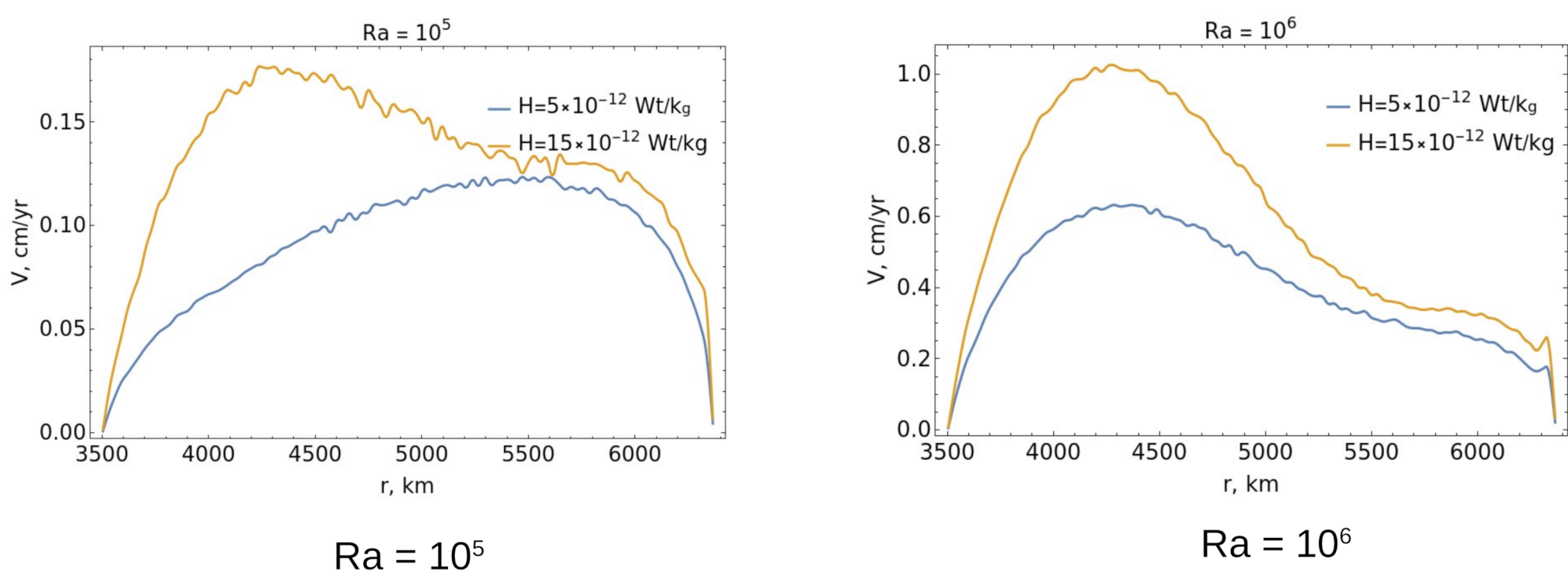
### Dependence of temperature T on depth r for different amounts of 40 K concentration



$Ra = 10^5$

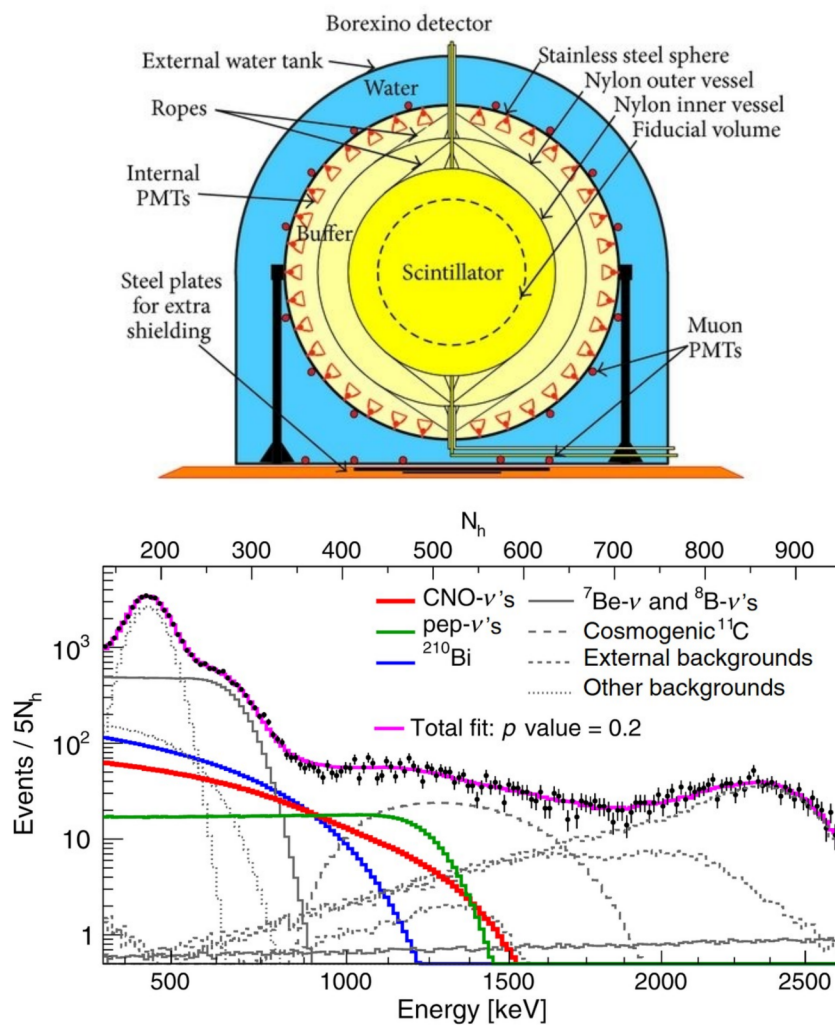
$Ra = 10^6$

### Dependence of mean convection velocity V cm/yr on depth r for different amounts of 40 K concentration



$Ra = 10^5$

$Ra = 10^6$



- Overburden 4200 m.w.e.
- Liquid scintillator volume 315 m3 placed in thin (125 um) nylon film.
- Single events from neutrinos and antineutrinos are detected. Mainly from the Sun
- Due to radioactive containment of the film sensitive volume was decreased down to 73 t.

Borexino measurement result in 2022.

$R_{\text{CNO}} = 6.7$  events per d/100 tons

### Estimation of heat flow from <sup>40</sup>K

Potassium makes up about 2.6% of the weight of the Earth's crust.

High neutrino count rate from <sup>40</sup>K in data Borexino indicates its high abundance throughout the Earth.

Taking into account its isotopic abundance 0.0117%, the total amount of potassium in the all Earth is 3.2%.

$$m(^{40}\text{K}) = 2.1 \cdot 10^{22} \text{ g}$$

$$H = (m(^{40}\text{K}) \cdot N_a \cdot E_{\text{release}} \cdot \alpha) / (A \cdot \tau),$$

where  $N_a$  - Avogadro number,  $A$  - atomic number,  $E_{\text{release}} = 0.6$  MeV - average energy release in <sup>40</sup>K decay,  $\tau = t_{1/2} / \ln 2$  - mean lifetime of isotope,  $\alpha$  - the conversion factor 1 MeV =  $1.6 \cdot 10^{-13}$  J

This amount of <sup>40</sup>K results in a total heat flow of about **600 TW!**

While the entire heat flow of the Earth is **47 TW**

**The question arises:**  
**how does the increased content of radioactive potassium affect the Earth's thermal balance?**

### Initial and boundary conditions

#### Simulation parameters

- $\alpha_0 = 2 \times 10^{-5} \text{ K}^{-1}$
- $\rho = 4.5 \times 10^3 \text{ kg/m}^3$
- $D = 2900 \text{ km}$
- $\Delta T = 3700 \text{ K}$
- $\eta_0 = 5 \times 10^{21} \text{ Pa}\cdot\text{s}$
- $\kappa = 10^{-5} \text{ m}^2/\text{s}$
- $c_p = 1.25 \times 10^3 \text{ J/(kg K)}$
- $Ra = 10^5$  and  $Ra = 10^6$

Heat sources from <sup>40</sup>K inside the mantle

$$H(t) = H_0 \cdot \exp(-t/t_{40K})$$

, where  $H_0 = H_{\text{now}} \cdot \exp(t_{\text{max}}/t_{40K})$

- Low <sup>40</sup>K concentration  $H_{\text{now}} = 5 \times 10^{-12} \text{ W/kg}$  **20 TW**
- High <sup>40</sup>K concentration  $H_{\text{now}} = 15 \times 10^{-12} \text{ W/kg}$  **60 TW**

No leakage condition  
 $\mathbf{V}|_{r=0} = \mathbf{V}|_{r=D} = 0$

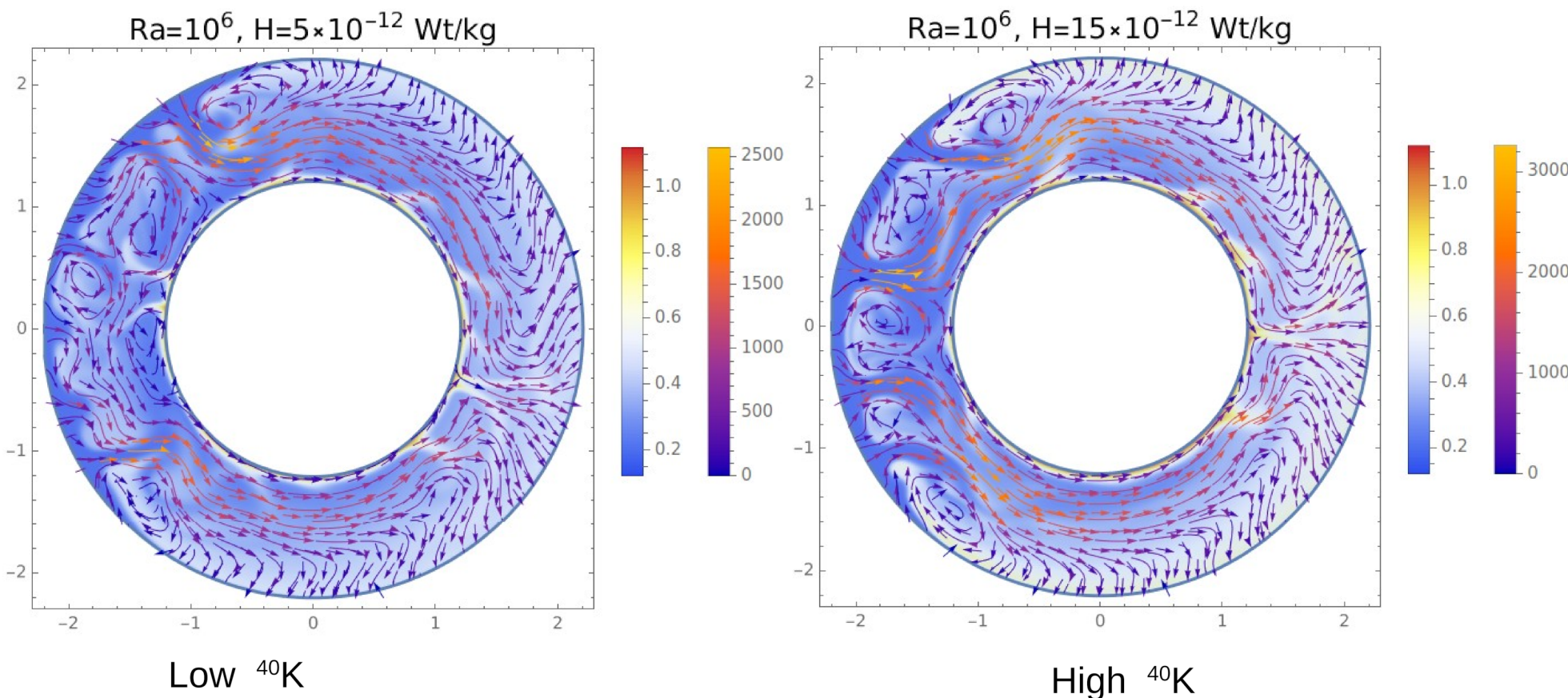
Temperature at the mantle-crust boundary  
 $T|_{r=0} = 0.12 \Delta T = 420 \text{ K}^0$

Temperature at the mantle-core boundary  
 $T|_{r=D} = 1.12 \Delta T = 3920 \text{ K}^0$

Initial conditions  
 $\mathbf{V} = 0$   
 $T = \Delta T = 3500 \text{ K}^0$

$t_{\text{max}} = 4500 \text{ Myr}$

### Results of mantle convection modeling for $Ra = 10^6$



## Discussion and conclusion

- We provide the indication of high flux of 40 K geo-antineutrino and geo-neutrino (40 K-geo-( $\bar{\nu} + \nu$ )) with Borexino Phase III data
- Large geoneutrino flux from 40 K indicates low metallicity of the Sun
- The abundance of potassium in the range 2 - 4% from the Earth mass can give such flux.
- We modeled the heat distribution in the Earth taking into account the heat from the high 40 K concentration.
- At sufficiently large Rayleigh numbers, excess heat from 40 K is transferred to mantle convection.

